

The Steps Along The Way Whereby Einstein's General Theory Enabled The Rise of Present Day Cosmology

George Ellis

University of Cape Town

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Institut Henri Poincaré, Paris

General Relativity enabled cosmology

Key steps on the way

① Consistent cosmological models

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- 2 Curvature and topology of space

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- 7 Structure formation and inhomogeneity
- 8 Gravitational lensing
- 9 A coherent picture?

1: Consistent cosmological models

General relativistic before Newtonian

Problems with Newtonian models

(Newton? Laplace? Seeliger (1895) inconsistent: divergences)

Einstein static universe model (1917):

Local gravity everywhere \Rightarrow consistent universe model

Gravity curves spacetime.

Static ($\Lambda > 0$): taken for granted by all

But unstable (Eddington)

(Generalized) Newtonian models much later

Milne and Mcrea: consistent Newtonian model (1934)

Heckmann and Schücking: spatially homogeneous?

$\text{Accn} = \{\text{acceleration} + \text{inertia}\}$, new conditions at infinity

2: Curvature and topology of space

Geometry as physics

Positively and negatively curved 3-spaces

$$ds^2 = -dt^2 + a^2(t)\{dr^2 + f^2(r)d\Omega^2\} \quad (1)$$

in comoving coordinates: $u^a = \delta_0^a$, where $a(t)$ is the scale factor and

$$f(r) = \{\sin(r), r, \sinh(r)\} \text{ if } k = \{+1, 0, -1\}$$

The spatial sections need not be flat. Euclid is undermined:
Matter curves space (Gauss-Codazzi equations + EFE).

Then $k = +1$ necessarily implies closed spatial sections;

However $k = 0, -1$ allow closed spatial sections.

The topology need not be simply connected.

Indeed infinite possibilities if $k = -1$.

Space and spacetime

Preferred 4-velocities

In the real universe: there is always a preferred 4-velocity field $u^a(x^j)$: $u^a = dx^a/ds$, $u^a u_a = -1$ (Weyl, Ehlers). For example:

- The average motion of matter
- The Cosmic Background Radiation frame (the CBR is isotropic)
- The Ricci Eigenframe: $R_{ab}u^a = \lambda u_b$

In a Robertson-Walker geometry, they all coincide.

Generically (e.g. perturbed FLRW): the last.

Then: space and time are split into space and time by u^a , h_{ab} where

$$h_{ab} := g_{ab} + u_a u_b \Rightarrow h_a^b h_b^c = h_a^c, h_{ab} u^b = 0, h^a_a = 3$$

Then $X_{||} = X_a u^a$, $X_{\perp}^b = X_a h^{ab}$, $\dot{X}^a = X_{a;b} u^b$, $D_a X_b = h_a^c h_b^d X_{d;c}$

The problem with de Sitter and Anti-de Sitter spaces: no preferred 4-velocity (spacetimes of constant curvature: Schrödinger).

3: The expanding and evolving universe

Geometry as physics: gravity governs spacetime of cosmology

Non-static models: Dynamic geometry, scale factor $a(t)$
(Friedmann, Lemaître: not Einstein!)

Raychaudhuri equation (gravitational attraction)

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3} \left(\rho + \frac{3p}{c^2} \right) + \frac{\Lambda c^2}{3} \quad (2)$$

Friedmann equation (energy equation)

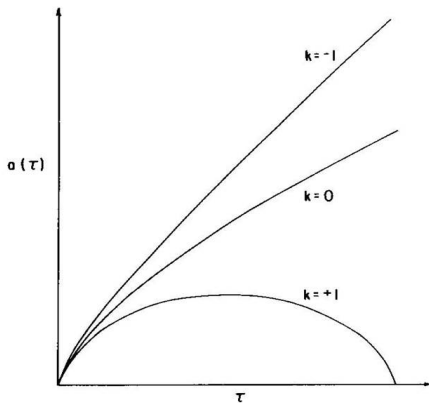
$$\frac{\dot{a}^2}{a^2} = \frac{8\pi G \rho}{3} + \frac{\Lambda c^2}{3} - \frac{kc^2}{a^2} \quad (3)$$

Conservation equation (consistency)

$$\dot{\rho} + 3\frac{\dot{a}}{a}(\rho + p) = 0 \quad (4)$$

Equation of state $p = p(\rho)$: matter drives geometry

The basic dynamics (Robertson 1933)



Singular start, then competition between KE and PE.

Spatial curvature linked to recollapse: $\Omega := 8\pi G\rho/3H^2$ takes value $\Omega = 1$ for the critical case, where $H(t) := \dot{a}(t)/a(t)$.

More complex when $\Lambda \neq 0$: static and asymptotic models possible.

4: A start to the universe

Singularity theorems

Energy conditions

$$\rho + \frac{3p}{c^2} \geq 0 \quad (5)$$

$$\rho + \frac{p}{c^2} \geq 0 \quad (6)$$

implies a singularity a finite time $t_0 < (1/H_0)$ ago if $\Lambda \leq 0$:

$$\{H_0 > 0, \Lambda \leq 0\} \Rightarrow \left[\lim_{t \rightarrow t_0} a(t) = 0, \lim_{t \rightarrow t_0} \rho(t) = \infty \right] \quad (7)$$

A crisis for physics: a start to time, space, and physics itself
[Wheeler]

Singularity Theorems

Hawking and Penrose

Basis: General Raychaudhuri equation (Ehlers)

$$\dot{\Theta} + \frac{1}{3}\Theta^2 + 2(\sigma^2 - \omega^2) - \dot{u}^a{}_{;a} + \frac{1}{2}\kappa(\rho + 3p/c^2) - \Lambda = 0. \quad (8)$$

But direct methods (even in Bianchi models) cannot prove no singularity.

Global methods: Penrose (1965), Hawking (1966)

Domain of dependence, Boundary of future, Null Raychaudhuri equations
 \Rightarrow singularities must exist (type not determined) provided energy conditions satisfied

Inflation and scalar fields: a reprieve?

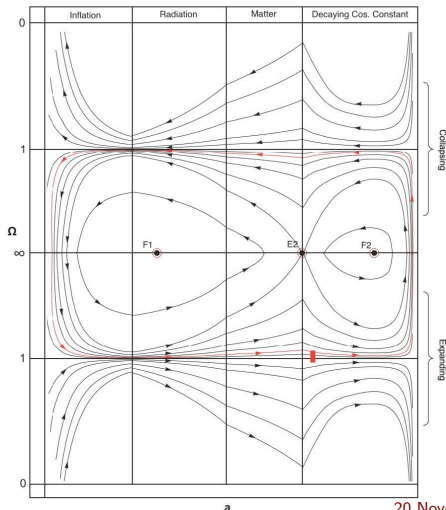
$$\rho = \frac{1}{2}\dot{\phi}^2 + V(\phi), \quad p = \frac{1}{2}\dot{\phi}^2 - V(\phi) \quad (9)$$

So $\rho + 3p = 2\dot{\phi}^2 - 2V(\phi)$ can be negative if potential dominated.

Cyclic models possible for standard GR

[arXiv:1511.03076]

If we have $k = +1$ and a decaying cosmological constant ... Ω versus $a(t)$



5: Null cone observational tests

Cosmology as science

Lightrays and photons

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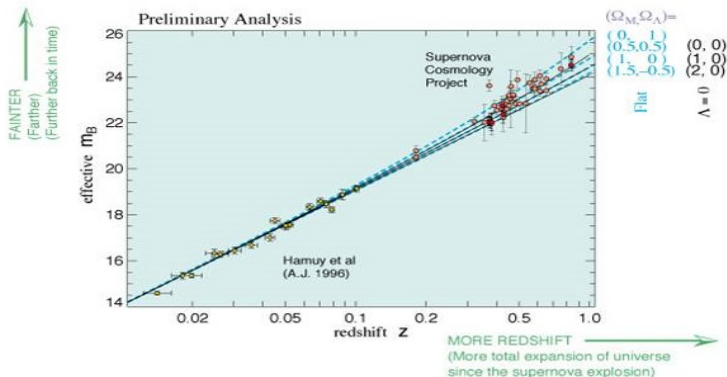
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- An accelerating universe

The supernova data

SN1a as standard candles:

Hubble Plots



The universe is presently accelerating
 \Rightarrow Dark energy is present: $\rho + 3p/c^2 < 0$.

6: Observational and causal limits: horizons

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limit causality

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Limit observations

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Limit observations
- Event horizons:
The far future:
Nothing about observations in cosmology.

6: Observational and causal limits: horizons

Refocussing of the past light cone

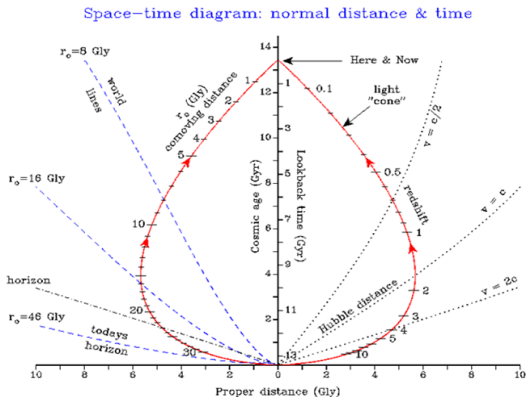


Figure: *Refocussing of Past Light Cone* [Ned Wright]

6: Observational and causal limits: horizons

Horizons: Penrose conformal diagram

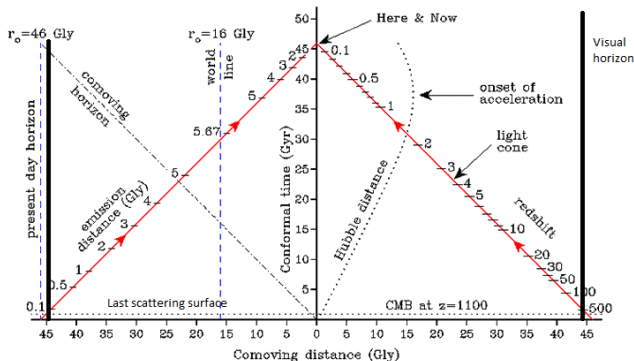


Figure: *Past Light Cone in conformal coordinates* [Ned Wright].
Particle horizon (causal limit) and visual horizon (observational limits)

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Gravitational attraction forms structure: Perturbation equations

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- Interactions: CMB polarisation

The gauge problem

The issue

One can choose a constant time surface $\{t = \text{const}\}$ so as to make a density inhomogeneity

$$\delta\rho(t, x^i) := \rho(t, x^i + \delta x^i) - \rho(t, x^i) \quad (10)$$

vanish: simply choose $\{t = \text{const}\}$ surfaces to be the same as the $\{\rho = \text{const}\}$ surfaces, then

$$\rho(t, x^i + \delta x^i) = \rho(t, x^i) \Rightarrow \delta\rho = 0.$$

Indeed the value determined for $\delta\rho(t, x^i)$ is arbitrary because of the coordinate freedom $t \rightarrow t' = t'(t, x^i)$ allowed by General Relativity. This allows apparent density variations that are in fact gauge modes.

NB: this problem does not occur in Newtonian theory

Gauge invariant approaches

Bardeen; 1+3 covariant

Use Bardeen variables, or CGI variables (Hawking, Ellis and Bruni). This 3+1 gauge invariant and covariant formalism centres on the comoving fractional spatial density gradient, defined as

$$\mathcal{D}(\rho)_a := h_a^b \rho_{,b} / \rho \quad (11)$$

for an observer with 4-velocity u^a ($u_a u^a = -1$), where $h_{ab} := g_{ab} + u_a u_b$ projects orthogonal to u^a .

Sachs Theorem (Stewart and Walker): *any quantity which vanishes in the background spacetime is gauge invariant.*

1+3 CGI variables for geometrically preferred u^a (Ricci eigenvectors):

Fluid flow: acceleration \dot{u}^a , shear σ_{ab} , vorticity ω^a

Weyl tensor: E_{ab} , H_{ab} (Maxwellian equations)

Spatial Inhomogeneity: density $\mathcal{D}(\rho)_a$, pressure $\mathcal{D}(p)_a$, expansion $\mathcal{D}(\theta)_a$.

Perturbation equations

General relativity structure formation

Take the spatial gradient of the general form of Raychaudhuri's equation and the density conservation equation.

When $w = p/\rho = \text{const}$ and $\Lambda = 0$, the linearised growth equation for modes of wave number n obtained this way is

$$\ddot{\mathcal{D}}_a + \left(\frac{2}{3} - w\right)\theta \dot{\mathcal{D}}_a - \left(\frac{(1-w)(1+3w)}{2}\kappa\rho\right)\mathcal{D}_a - w\frac{n^2}{a^2}\mathcal{D}_a = 0 \quad (12)$$

which directly gives the general relativistic version of the Jeans' length (competition between gravitational attraction and restoring pressure) and the density perturbation growth laws. When $w = 0$ this reduces to

$$\ddot{\mathcal{D}}_a + \frac{2}{3}\theta \dot{\mathcal{D}}_a - \frac{1}{2}\kappa\rho\mathcal{D}_a = 0 \quad (13)$$

which directly gives Lifshitz' 1946 results for pressure free matter.

Kinetic theory

Interaction of matter and radiation

CGI relativistic kinetic theory

Photons, $p^a = E(u^a + e^a)$, $e^a e_a = 1$, $e^a u_a = 0$. Distribution function:

$$f(x^i, p^j, E) = f(x^i, E) + f(x^i, E)_a e^a + f(x^i, E)_{ab} e^a e^b + f(x^i, E)_{abc} e^a e^b e^c \dots$$

where $f(x^i, E)_{a_1 \dots a_N} = f(x^i, E)_{A_N}$ are PSTF tensors, $A_N := a_1 \dots a_N$.

Then with $p = \rho/3$ (radiation), T_{ab} is expressed entirely in terms of integrals of $f(x^i, E)$, $f_a(x^i, E)$ and $f_{ab}(x^i, E)$ as follows:

$$\rho = 4\pi \int_0^\infty E^3 F dE, \quad q^a = \frac{4\pi}{3} \int_0^\infty E^3 F^a dE, \quad \pi^{ab} = \frac{8\pi}{15} \int_0^\infty E^3 F^{ab} dE.$$

The matter stress tensor is

$$T_{ab} = \frac{1}{3}(4\rho u_a u_b + \rho g_{ab}) + q_{(a} u_{b)} + \pi_{ab}$$

the higher order terms do not enter the EFE.

The Boltzmann equations

Exact non-linear Boltzmann equations generally (except for the first few) link 5 consecutive moments $f(x^i, E)_{a_{N+2}, \dots, a_{N-2}}$ to a collision term:

$$\begin{aligned} E^{-1} b_{A_\ell} = & \dot{F}_{<A_\ell>} - \frac{1}{3} \theta E F'_{A_\ell} + D_{<a_\ell} F_{A_{(\ell-1)>}} + \frac{(\ell+1)}{(2\ell+3)} D^a F_a A_\ell \\ & - \frac{(\ell+1)}{(2\ell+3)} E^{-(\ell+1)} \left[E^{(\ell+2)} F_{aA_\ell} \right]' A^a - E^\ell \left[E^{1-\ell} F_{<A_{\ell-1}} \right]' A_{a_\ell} \\ & - \ell \omega^b \epsilon_{bc(a_\ell} F_{A_{\ell-1})}^c - \frac{(\ell+1)(\ell+2)}{(2\ell+3)(2\ell+5)} E^{-(\ell+2)} \left[E^{\ell+3} F_{abA_\ell} \right]' \sigma^{ab} \\ & - \frac{2\ell}{(2\ell+3)} E^{-1/2} \left[E^{3/2} F_{b<A_{\ell-1}} \right]' \sigma_{a_\ell}^b - E^{\ell-1} \left[E^{2-\ell} F_{<A_{\ell-2}} \right]' \sigma_{a_{\ell-1}a_\ell}. \end{aligned}$$

(dot is $\partial/\partial t$, prime is $\partial/\partial E$, $< .. >$ is PSTF part, b_{A_ℓ} is collision term).

[Maartens, Gebbie, Ellis: arXiv astro-ph/9808163;

Challinor, Lewis, Lasenby: arXiv:astro-ph/9911177].

The data: CMB power spectrum

Inflation predictions

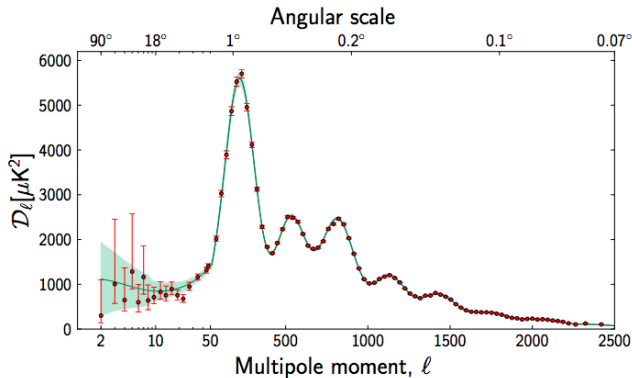


Figure: The CMB power spectrum (Planck)

The agreement of theory and observation (using observation to fix a theory parameter)

The data: Baryon Acoustic Oscillations

Inflation predictions

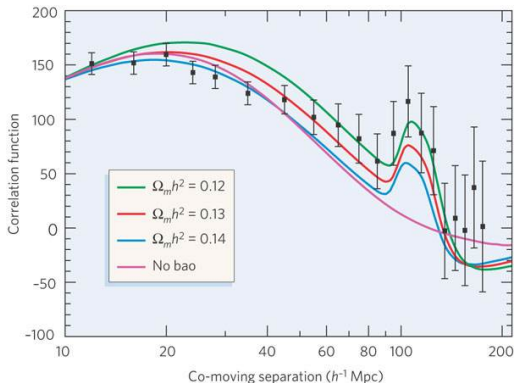


Figure: The matter power spectrum

The agreement of theory and observation (radiation and matter power spectra)

Validity of the Copernican Principle

Philosophy to Physics

Can we test the homogeneity of the universe?

Inhomogeneous models can explain SN1a results with no dark energy

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$$\Omega_k = \frac{[H(z)D'(z)]^2 - 1}{[H_0 D(z)]^2}$$

Constant, independent of redshift

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Constant, independent of redshift

- Time drift of cosmological redshift
- Kinetic SZ effect and CMB spectrum:
Probably rules models out

8: Gravitational lensing

The intervening screen

Bending of light by matter (Einstein 1915, 1936)

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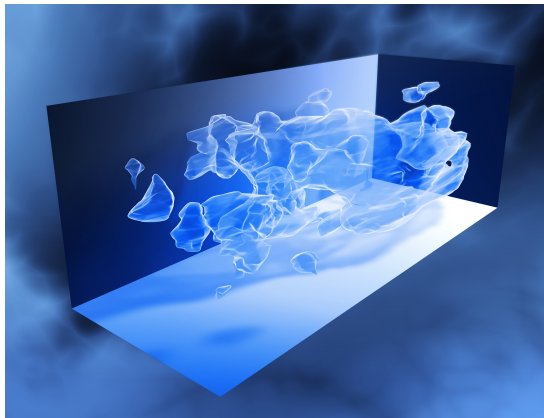
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- Lenses as telescopes:
Seeing further

A key cosmological tool

Lensing as a tool in cosmology

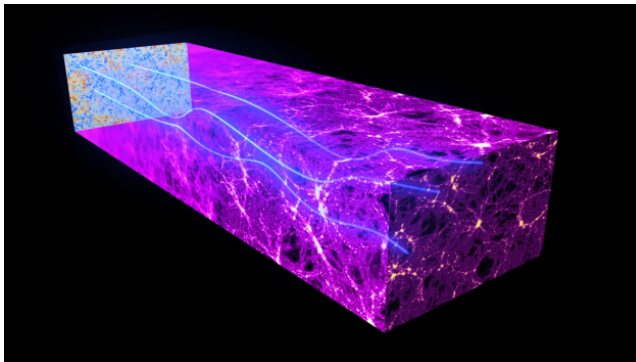
Mapping dark matter



Dark matter distribution - weak gravitational lensing (Hubble Space Telescope).

Lensing as a tool in cosmology

Affecting CMB observations



CMB photons are deflected by the gravitational lensing effect of massive cosmic structures. Data from the Planck satellite enables measuring gravitational lensing of the CMB over the whole sky.

9: A coherent picture?

Cosmic concordance

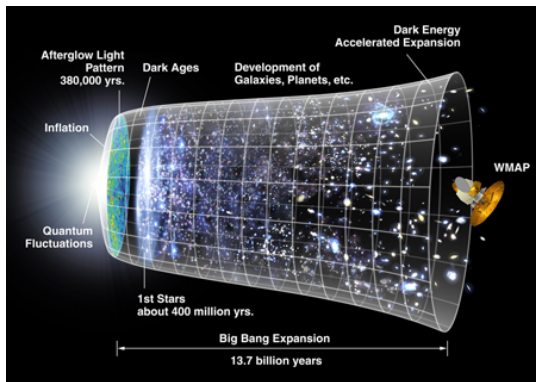


Figure: The stages of the universe (NASA)

The agreements

9: A coherent picture?

Issues

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Dark matter, dark energy, the inflaton
The right hand side of the Field Equations

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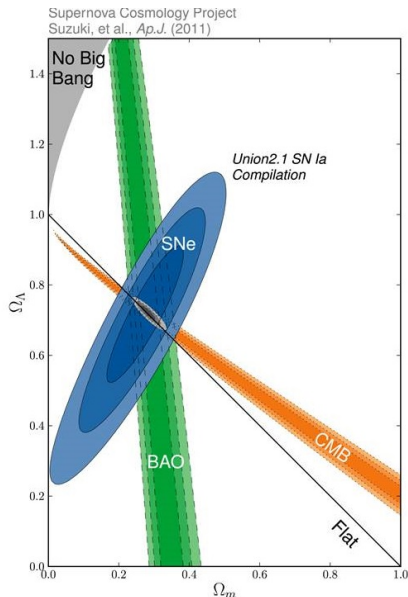
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- Small universes? - circles in the sky
- The most sensitive tests: structure formation:
CMB anisotropy: the effect of the universe on local physics

Testing the standard model

The supernova data is based on observing the background model geometry directly. The BAO data reflects how the background model has affected structure formation. The WMAP data represents how this structure affects the observed CMB temperature power spectrum.

It is the latter two, based in perturbations about the FLRW model, that together give us the best estimates of the cosmological parameters Ω_Λ , Ω_m .



Cosmology as physics

Successive Unifications

The series of unifications:
cosmology as progress in physical science

Cosmology as physics

Successive Unifications

The series of unifications:
cosmology as progress in physical science

- Gravity:
Apples, the Moon, and the universe
⇒ Gravity as geometry! (Einstein)

Cosmology as physics

Successive Unifications

The series of unifications:
cosmology as progress in physical science

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Apples, the Moon, and the universe
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- Quantum gravity and creation, quantum cosmology:
No solid ground. We can hypothesize with no real tests.

Conclusion: General relativity and cosmology

General relativity has made present day cosmology possible

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- Black holes
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- GPS systems

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The greatest development of the theory is not so much the background model as the perturbations about it. Handling the gauge issue is crucial.